

# Age distribution of the central stars of galactic disk planetary nebulae

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## ABSTRACT

**Context.** The determination of ages of central stars of planetary nebulae (CSPN) is a complex problem, and there is presently no single method that can be generally applied. We have developed several methods to estimate the ages of CSPN, based both on the observed nebular properties and in some properties of the stars themselves.

**Aims.** Our aim is to estimate the ages and the age distribution of CSPN and to compare the derived results with mass and age determinations of CSPN and white dwarfs based on empirical determinations of these quantities.

**Methods.** We discuss several methods to derive the age distribution of CSPN, namely, (i) the use of an age-metallicity relation that also depends on the galactocentric distance, (ii) the use of an age-metallicity relation obtained for the galactic disk, and (iii) the determination of ages from the central star masses obtained from the observed nitrogen abundances.

**Results.** We consider a sample of planetary nebulae in the galactic disk, most of which ( $\sim 69\%$ ) are located in the solar neighbourhood, within 3 kpc from the Sun. We estimate the age distribution of CSPN with average uncertainties of 1-2 Gyr, and compare our results with the expected distribution based both on the observed mass distribution of white dwarfs and on the age distribution derived from available mass distributions of CSPN.

**Conclusions.** We conclude most CSPN in the galactic disk have ages under 6 Gyr, and that the age distribution is peaked around 2-4 Gyr.

**Key words.** ISM: planetary nebulae – Stars: AGB and post AGB – Stars: fundamental parameters

## 1. Introduction

Planetary nebulae (PN) are the offspring of intermediate mass stars with main sequence masses between 0.8 and  $8 M_{\odot}$ , approximately. As a consequence, their properties reflect different physical conditions depending on the masses – and therefore ages – of their central stars (CSPN), which makes these objects extremely important in the study of the chemical evolution of the Galaxy (see for example Maciel et al. 2006). As an example, some recent theoretical models predict a time flattening of the observed radial abundance gradients in the galactic disk, while other models predict just the opposite behaviour. This can be analysed on the basis of abundance determinations in PN or in open cluster stars. In both cases, the results depend critically on the adopted ages of the objects considered.

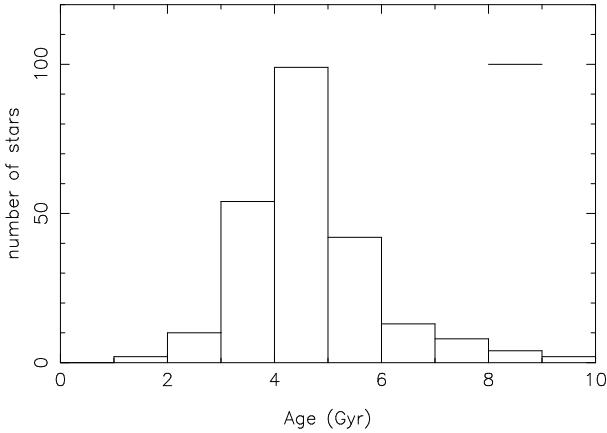
The determination of ages of CSPN is a complex problem, and there is presently no single method that can be generally applied. In fact, most accurately determined ages refer to relatively young objects, for which methods such as lithium depletion, activity or cluster membership can be applied (see for example Hillebrand et al. 2009). Our group has pioneered in the treatment of this problem, and we have developed several methods to estimate the ages of the PN progenitor stars, based both on the observed nebular properties and in some properties of the stars themselves (cf. Maciel et al. 2003, 2005a, 2006, 2008). According to Soderblom (2009), most age determination methods can be classified as (i) fundamental, (ii) model dependent, (iii) em-

pirical, and (iv) statistical. The methods discussed in this paper belong to the last class. In principle, the traditional methods to derive the ages of galactic stars can be applied to CSPN, such as the use of theoretical isochrones (see for example Idiart et al. 2007), particularly for extragalactic nebulae. On the other hand, the physical properties of these objects are not as well known as in the case of normal stars, so that the derived isochrones are generally uncertain, leading to the need of alternative methods.

In this work, we discuss three methods developed so far by our group, namely the use of (i) an age-metallicity relation that depends on the galactocentric distance (Section 2.1a), (ii) a simpler age-metallicity relation for the galactic disk (Section 2.1b), and (iii) the determination of ages from the central star masses obtained directly from the observed nitrogen abundance (Section 2.2). In Section 3, we estimate the expected age distribution of the CSPN based on (i) the observed mass distribution of white dwarf stars, and (ii) available mass distributions of CSPN, and compare the results with the distributions obtained by the methods mentioned above. In Section 4 a discussion is given, followed by some conclusions.

## 2. Age determination and distribution of CSPN progenitors from nebular abundances

2.1a. *Method 1: The age-metallicity-galactocentric distance relation*



**Fig. 1.** Age distribution of the central stars of planetary nebulae using an age-metallicity-galactocentric distance relation. The estimated age uncertainty is shown at the upper right corner.

The first method to be considered was initially developed by Maciel et al. (2003), in the framework of an estimate of the time variation of the radial abundance gradients in the galactic disk. Using the oxygen abundance measured in the nebula, which is given in the usual form  $\epsilon(O) = \log(O/H) + 12$ , the  $[O/H]$  abundance relative to the Sun is simply given by  $[O/H] = \log(O/H) - \log(O/H)_\odot$ , where we have adopted  $\epsilon(O)_\odot = 8.7$  (see for example Asplund 2003 and Asplund et al. 2004). The relation between the metallicity  $[Fe/H]$  and the oxygen abundance is given by

$$[Fe/H] = 0.0317 + 1.4168 [O/H], \quad (1)$$

which is valid for  $-1.0 < [Fe/H] < 0.5$ , as discussed by Maciel et al. (2003). Finally, the ages of the PN progenitor stars are given by an age-metallicity-galactocentric distance relation developed by Edvardsson et al. (1993),

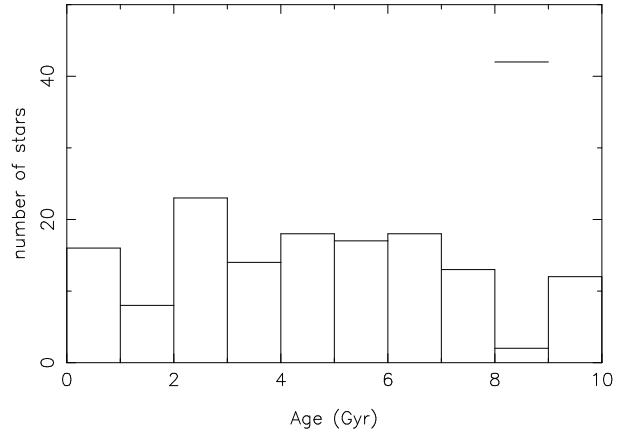
$$\log t = 0.872 - 0.303 [Fe/H] - 0.038 R, \quad (2)$$

where  $t$  is in Gyr, and  $R$  is the galactocentric distance in kpc, so that some knowledge of the distance to the PN must be assumed. These relationships were applied to a sample of 234 well observed PN from Maciel et al. (2003), located in the solar neighbourhood and in the galactic disk, for which the data are obtained with the highest accuracy. These objects have galactocentric distances in the range  $4 < R(\text{kpc}) < 14$ , and most (69%) are located in the solar neighbourhood, with distances  $d \leq 3$  kpc. The results are shown in Fig. 1. It can be seen that the distribution shows a prominent peak, located around 3-6 Gyr, similar to the age of the Sun, suggesting that most PN come from stars having masses close to one solar mass when in the Main Sequence.

#### 2.1b. Method 2: The age-metallicity relation for the galactic disk

Rocha-Pinto et al. (2000) derived an age-metallicity relation for the galactic disk based on chromospheric ages and accurate metallicities. According to this relation (cf. Table 3 of Rocha-Pinto et al. 2000), we can write

$$[Fe/H] = 0.13969 - 0.08258 t + 0.00277 t^2 \quad (3)$$



**Fig. 2.** Age distribution of the central stars of planetary nebulae using the age-metallicity relation of Rocha-Pinto et al. (2000). The estimated age uncertainty is shown at the upper right corner.

where  $t$  is in Gyr. From this equation the stellar lifetimes can be determined once the metallicity is fixed. We can apply the same procedure as in the previous method (cf. Section 2.1a), and obtain  $[Fe/H]$  from the oxygen abundance  $\epsilon(O)$ . The results for the same sample considered in Fig. 1 are shown in Fig. 2. The derived age distribution is flatter than in the previous method, but in both cases most stars have ages under 6 Gyr.

#### 2.1c. Uncertainty analysis

Oxygen abundances are the best determined abundances in PN, with uncertainties typically under 0.2 dex, while other elements have generally higher uncertainties, in the 0.2 to 0.3 dex range. In the case of the best determined O/H abundances, formal uncertainties under 0.10 dex are often estimated. The objects included in our sample are all disk planetary nebulae, avoiding the more distant objects for which the abundances are poorly known. They result from a very careful selection, in which the best spectra available were taken into account, and for which a comparison of abundances from different sources produces a very good agreement (see for example the individual abundance comparisons shown in Maciel et al. 2006). All abundances considered are derived from collision excitation lines, which are considered as true representatives of the ionized gas in the nebulae (cf. Liu 2006). An additional uncertainty may be introduced by the ON conversion which may occur in the progenitor stars (cf. Stasińska 2008). However, present results are not conclusive, and in any case they would only affect the progenitor stars near the upper mass bracket of the Main Sequence stars that produce planetary nebulae, which are a small fraction of the sample considered here.

The solar oxygen abundance is accurate within 0.05 dex (see for example Asplund et al. 2006), so that the uncertainty in the derived  $[O/H]$  abundances is essentially the same as in  $\epsilon(O)$ . On the other hand, from the correlations presented in Maciel et al. (2003), iron and oxygen are clearly in lockstep in the galactic disk, so that we can safely adopt this hypothesis for our present sample. The average uncertainty in the  $[Fe/H]$  metallicity is dominated by the uncertainty in the  $[O/H]$  ratio, which is essentially the same as in the  $\epsilon(O)$  abundance, since the uncertainties in the slope and intercept of Eq. (1) are small, corresponding to 0.049

and 0.016, respectively. Therefore, an upper limit of about 0.3 dex can be estimated for the uncertainty in [Fe/H], but a more realistic average would be about 0.2 dex, which corresponds to an O/H uncertainty of roughly 0.2 dex.

Concerning the ages as given by Eq.(2), a similar procedure taking into account the [Fe/H] uncertainties leads to age uncertainties in the range 0.5 to 1 Gyr for objects in the solar neighbourhood, which are the majority in the sample considered here.

The term involving the galactocentric distance provides a further uncertainty, but the range estimated above is not significantly changed. The abundances themselves are distance-independent, but distance uncertainties may affect the galactic abundance gradients and as a secondary effect the position of the nebula projected onto the galactic plane. Independent confirmation of the reality of the gradients are presented by Peña et al. (2005), where a new method to determine the distances was developed, leading to a clear disk gradient that flattens out in the inner galaxy, a result confirmed by Pottasch and collaborators (cf. Gutenkunst et al. 2008). The main uncertainties in the gradients were discussed in detail by Maciel et al. (2005b), and the effect of the adopted distances was also analyzed by Maciel et al. (2006) and more recently by Maciel & Costa (2009). In the latter work, we have taken into account four different PN distance scales, our own Basic Sample, and the scales by Cahn et al. (1992), Zhang (1995), and Stanghellini et al. (2008). The main conclusion is that there is no appreciable change in the gradients when a sample of over 200 nebulae are considered with central stars in the age range of 2 to 10 Gyr. It was also shown that, in average, the galactocentric distances obtained by these scales do not differ by more than about 1 kpc for objects in a ring centered at the solar position ( $R_0 \simeq 7.5 - 8.0$  kpc) and extending to about 3 kpc in either direction, which includes most nebulae in our sample.

In agreement with these results, a typical uncertainty of  $\sigma(\log t) \simeq 0.10$ , where  $t$  is in Gyr, was estimated from the analysis by Edvardsson et al. (1993), on which Eq. (2) is based. Therefore, the age distribution of Fig. 1 may be displaced by about 1 Gyr in either direction. Taking into account the observed scatter in the age-metallicity relation, this uncertainty is probably larger, up to about 0.2 dex (see a detailed discussion in Rocha-Pinto et al. 2000, 2006). As a consequence, absolute *individual* ages may have uncertainties higher than 1 Gyr, but it should be stressed that here we are interested in the *age distribution*, so that an actual displacement of the histogram of Fig. 1 by about 1 Gyr, as indicated by the horizontal bar at the upper right corner of the figure, is a realistic estimate.

Considering now the uncertainties involved in the approximation given by Eq.(3), we would like to stress that an age-metallicity relation is expected in the framework of a simple model of galactic chemical evolution (cf. Prantzos 2008), and in fact several independent investigations have been able to derive some working relationships in the last two decades (cf. Rocha-Pinto et al. 2000 and references therein; Bensby et al. 2004). However, some problems are still under discussion, particularly the observed dispersion of this relation and its applicability to the thick and/or thin disks. The observed dispersion depends critically on the samples considered, and from the results by Edvardsson et al. (1993) and Feltzing et al. (2001), a relatively large dispersion of about 0.3 dex was estimated for the [Fe/H] ratio.

Our own results indicate that the actual dispersion may be considerably lower, about 0.2 dex (Rocha-Pinto et al. 2000, 2006), provided some important corrections are made, concerning the cosmic scatter, incompleteness of the samples and a careful analysis of stars that present contradictory age indicators, as discussed in detail by Rocha-Pinto et al. (2002). This value agrees very well with our estimate of the formal uncertainty, as discussed above. Therefore, the similarity of the uncertainties of the methods discussed in Sections 2.1a and 2.1b are reinforced, and the average age uncertainty of 1 Gyr is shown as a horizontal bar at the upper right corner of Fig. 2. These results are supported by a recent analysis by Prantzos (2008), who presented a detailed discussion on the local age-metallicity relation based on the results of the Geneva-Copenhagen Survey (cf. Nordström et al. 2004). The resulting relationship shows a decrease in the metallicities with increasing ages, as expected, up to about 6 Gyr, remaining essentially flat at later epochs. Taking into account the biases affecting this relation by using simulated data as input for the age-metallicity relation, a monotonic relation was obtained, up to about 10 Gyr ago, in better agreement with the views expressed in our previous work.

## 2.2. Method 3: The age-N/O mass relation for CSPN

### 2.2a. The age-N/O mass relation

This method was also employed by Maciel et al. (2003), and assumes a relationship between the central star mass  $m_{CS}$  and the N/O abundance (for details see Maciel et al. 2003), which is expected from several theoretical and observational analyses. The adopted relation can be written as

$$m_{CS} = 0.7242 + 0.1742 \log(\text{N/O}) \quad (4)$$

for  $-1.2 < \log(\text{N/O}) < -0.26$ , and

$$m_{CS} = 0.825 + 0.936 \log(\text{N/O}) + 1.439 [\log(\text{N/O})]^2 \quad (5)$$

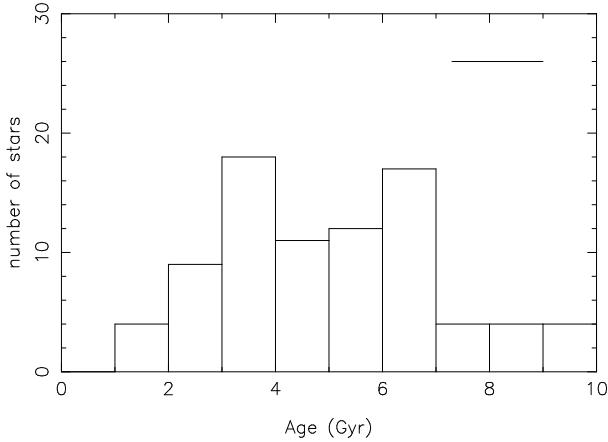
for  $-0.26 < \log(\text{N/O}) < 0.20$ . In these equations  $m_{CS}$  is in solar masses. In order to obtain the stellar masses on the main sequence ( $m_{MS}$ ), we adopted an initial mass-final mass relation of the form

$$m_{CS} = a + b m_{MS} + c (m_{MS})^2, \quad (6)$$

where  $a = 0.47778$ ,  $b = 0.09028$ , and  $c = 0$ , to reproduce the same values in Maciel et al. (2003), namely  $m_{CS} = 0.55 M_{\odot}$  for  $m_{MS} = 0.8 M_{\odot}$  and  $m_{CS} = 1.2 M_{\odot}$  for  $m_{MS} = 8 M_{\odot}$ , which reflect the known ranges of both CSPN and their progenitor stars on the main sequence. Concerning the mass-age relation, an approximation generally considered as accurate can be written as

$$\log t = d + e \log m_{MS} + f (\log m_{MS})^2. \quad (7)$$

where  $t$  is the Main Sequence lifetime, or age, measured in Gyr, and the Main Sequence mass  $m_{MS}$  is given in solar masses. There are many discussions in the literature which suggest different values for the constants  $d$ ,  $e$ ,  $f$  (see for example Romano et al. 2005), so that we will consider two cases here. In the first case, which we call Case A, we have  $d = 1.0$ ,  $e = -2.0$  and  $f = 0.0$ , which corresponds to a relation of the form  $t = C/m_{MS}^2$ , where  $C = 10 M_{\odot}^2$  Gyr.



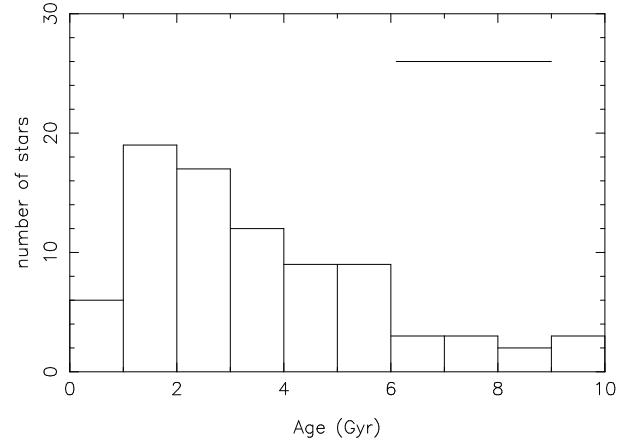
**Fig. 3.** Age distribution of the central stars of planetary nebulae using a mass-N/O abundance relation (Case A). The estimated age uncertainty is shown at the upper right corner.

The second case, which we call Case B, adopts the well known mass-age relation by Bahcall & Piran (1983), which corresponds to  $d = 1.0$ ,  $e = -3.6$ , and  $f = 1.0$  in Eq. (7). Again we have  $t = 10$  Gyr for  $m_{MS} = 1M_{\odot}$ . Taking into account Cases A and B has two advantages: first, it stresses that this important relation still involves some uncertainties; and second, the relation considered as Case B gives a steeper decrease of the stellar lifetimes at larger masses compared to Case A, so that we can easily interpret the behaviour of the age distributions as a function of the mass-age relationship.

Method 3 was applied to a sample of 122 PN for which all necessary data was available (cf. Maciel et al. 2003). Again we selected disk planetary nebulae for which the best abundance data were available so as to keep the uncertainties to a minimum. The results are shown in Figs. 3, and 4 for cases A and B, respectively. These results are similar to the age-metallicity-radius method, in the sense that most objects have ages lower than about 10 Gyr, and there is a sharp maximum in the probability distribution. However, its location depends on the estimated lifetimes as a function of the Main Sequence mass, being around 3-7 Gyr for Case A and 1-4 Gyr for Case B. From case A to case B the lifetimes of the more massive stars are decreased, so that the probability of finding stars at larger lifetimes decreases, and the whole peak moves to the left, as shown by Figs. 3 and 4.

## 2.2b. Uncertainty analysis

An estimate of the uncertainties involved in Method 3 suggests that they are similar or somewhat larger than in Methods 1 and 2. The basic relation is given by Eqs.(4) and (5), which relate the central star masses and the N/O abundances. Although such a relation is expected from theoretical models (see for example Renzini & Voli 1981, Marigo 2000, 2001, Perinotto et al. 2004), there is presently no *clearcut* functional dependence between these quantities, which led Cazetta & Maciel (2000) and Maciel (2000) to propose a calibration based on the best parameters available. The N/O ratio is relatively well determined, with uncertainties similar to the O/H ratio or even better, namely, under 0.2 dex, as already discussed. Adopting this value



**Fig. 4.** The same as Fig. 3 for Case B.

and also taking into account the uncertainties in the coefficients of Eqs. (4) and (5), an upper limit of about  $0.2 M_{\odot}$  would be obtained for the mass uncertainty. However, a more realistic estimate would be lower than this value, as suggested by the recent application of N/O masses to a well studied sample of CSPN by Maciel et al. (2008).

In that work, the derived masses were successfully compared with the known mass distributions of CSPN and white dwarf stars in order to explain the relationship between the modified momentum of the CSPN winds and the stellar luminosity. Some additional support to the N/O masses comes from the reanalysis of Tinkler & Lamers (2002) of the central star masses determined by Kudritzki et al. (1997). These results were based on an homogeneous set of parameters obtained from Zanstra temperatures, dynamical ages and evolutionary tracks. The average masses obtained by Tinkler & Lamers (2002) for the same sample studied by Maciel et al. (2008) and the N/O masses are in very good agreement. In view of these considerations, an average uncertainty closer to  $0.1 M_{\odot}$  would be more appropriate to Eqs. (4) and (5).

Considering now the initial mass-final mass relation as given by Eq.(6), there are many determinations of this relation in the literature (Vassiliadis & Wood 1993, Marigo 2000, 2001, Marigo & Girardi 2007, Meng et al. 2008), which generally agree with each other within 0.1 to  $0.2 M_{\odot}$ , so that the total uncertainties in the stellar masses are probably not much affected by this relation. As a consequence, the average uncertainties in the *individual* CSPN ages correspond to a mass uncertainty of at most  $0.2 M_{\odot}$ . In fact, the main contribution to the age uncertainty is due to the age estimates as given by Eq.(7), and at this point the best procedure to overcome such difficulty is to adopt some kind of parametrization, by considering cases A and B. Applying the mass uncertainty mentioned above, a formal age uncertainty would be about 3.1 and 4.7 Gyr for cases A and B, respectively, considering a typical star of one solar mass at the Main Sequence. These values can be considered as upper limits, as they were obtained using a  $0.2 M_{\odot}$  mass uncertainty. Adopting the more reasonable value of about  $0.1 M_{\odot}$ , the average uncertainties would be 1.7 Gyr and 2.9 Gyr for Cases A and B, as shown by the error bars in Figs. 3 and 4. Again, it should be stressed that we are interested in the *age distribution*, rather than in individual ages, so

that the general effect of the uncertainties is expected to be smaller than indicated by the formal uncertainties.

### 2.2c. Binary CSPN

A final comment is appropriate on Method 3, concerning the possibility that a significant fraction of the PN may have originated from close binary stars. Current results are controversial, in the sense that a very small number of binary PN are known, as discussed by De Marco (2009), while some investigations suggest that binaries constitute a much larger proportion of the galactic nebulae (see for example Miszalski et al. 2009, De Marco 2006, 2009, Moe & De Marco 2006). In view of these contradictory aspects, it is difficult to evaluate the effect of binarity on the present results. It would be expected that the age distribution would be displaced towards higher ages by only a small amount, as suggested by the good agreement of the results of our methods with the actual mass distribution of CSPN and white dwarf stars, as we will see in the next section.

## 3. The expected age distribution of the central stars of planetary nebulae

### 3.1. The white dwarf mass distribution

The expected age distribution of the CSPN can be estimated by analyzing the much better known mass distribution of the white dwarf stars. Since the average mass loss rates during the PN phase amount to about  $dM/dt \sim 10^{-8}$  to  $10^{-6} M_{\odot}/\text{yr}$  and the whole PN phase duration is about  $\Delta t \sim 1$  to  $2 \times 10^4 \text{ yr}$ , the total mass lost during this phase is  $\Delta m \sim (dM/dt) \Delta t \sim 10^{-4}$  to  $2 \times 10^{-2} M_{\odot}$ , which is much smaller than the CSPN masses. Therefore, as a first approximation, the mass distribution of the CSPN must be similar to that of the white dwarfs, except for the very low mass stars with  $m < 0.55 M_{\odot}$ . Such stars are not expected from theoretical models, since main sequence stars leading to white dwarfs with masses lower than about  $0.55 M_{\odot}$  probably go directly to the white dwarf phase.

Recent work on the mass distribution of white dwarfs by Madej et al. (2004) and Kepler et al. (2007) lead to a distribution which is strongly peaked at about  $0.56 M_{\odot}$ , as shown in Fig. 5 (cf. Madej et al. 2004). This investigation was based on a large sample of about 1200 white dwarfs, and shows very few objects (about 5%) with masses larger than about  $0.8 M_{\odot}$ .

The white dwarf mass distribution can be well fitted by a Gaussian probability density distribution defined by

$$P(m) = \frac{N(m)}{N_t} \frac{1}{\Delta m} \quad (8)$$

where  $N(m)$  is the number of stars with mass  $m$ ,  $N_t$  is the total number of stars, and  $\Delta m = 0.025 M_{\odot}$  is the size of the adopted mass bins, as shown in Fig. 5, where the curve plotted is  $30 \times P(m)$ . As can be seen, the gaussian fit to the data is good, although at very small and very large masses the predictions are somewhat lower than observed. Such probability is normalized, that is,  $\int P(m) dm = 1$ . For white dwarfs  $P(m)$  can then be written as

$$P(m) = \frac{A}{\sigma \sqrt{2\pi}} e^{-\frac{1}{2} \left( \frac{m-\mu}{\sigma} \right)^2}, \quad (9)$$

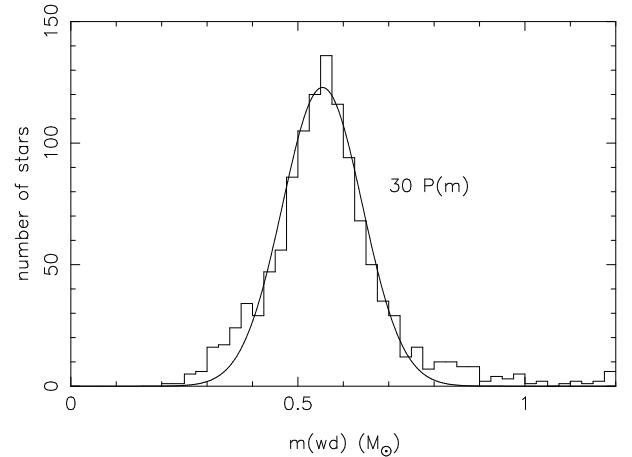


Fig. 5. Mass distribution of white dwarfs (Madej et al. 2004) and Gaussian fit.

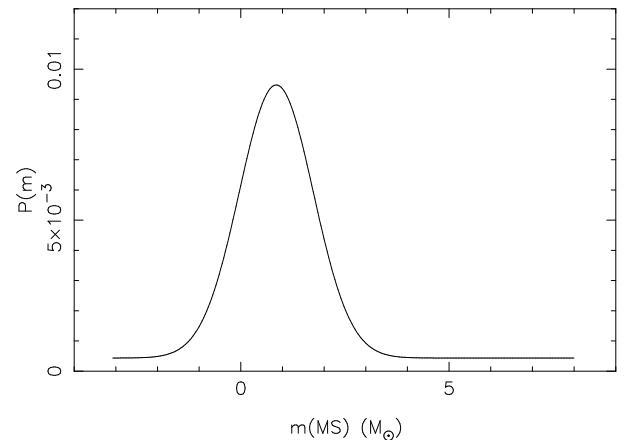


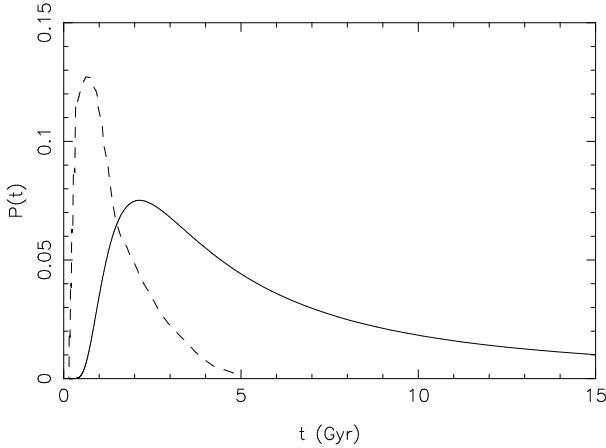
Fig. 6. Mass distribution of CSPN progenitor stars at the Main Sequence.

where  $A = 0.90349$ ,  $\sigma = 0.08798$  and  $\mu = 0.55420$ . Assuming that the CSPN have approximately the same mass distribution than the white dwarfs, we have  $P_{CS}(m) dm = P_{WD}(m) dm$ . As a first approximation, we can assume a linear relation between the CSPN mass and the Main Sequence (MS) mass, as given by Eq. (6) with  $c = 0$ , so that we have then  $a = 0.47778$  and  $b = 0.09028$ , as before. The main sequence masses can be written as

$$m_{MS} = \frac{1}{b} (m_{CS} - a) \quad (10)$$

and  $dm_{CS} = b dm_{MS}$ , so that the probability distribution for MS stars can be written as  $P_{MS}(m) = b P_{CS}(m)$ . The derived probability distribution of MS stars is shown in Fig. 6. It can be seen that it peaks around one solar mass, and also includes some very low (even negative) masses, which of course are unrealistic, as they correspond to CSPN masses lower than  $m_{CS} = a \simeq 0.48 M_{\odot}$ , which are not observed. However, as we will see later on, this essentially increases the probability of very high lifetimes, an effect that can be interpreted with some modifications in the calculation of the probability  $P_{MS}(m)$ .

Assuming that the star formation rate in the Galaxy has remained approximately constant along the galactic lifetime, the age distribution of the CSPN can be estimated



**Fig. 7.** Age distribution of the progenitors of the central stars of planetary nebulae. Solid line: case A, dashed line: Case B.

from the mass distribution of their progenitor stars. In order to derive the age distribution of the observed CSPN, we will adopt cases A and B considered previously. Considering that  $P(t) dt = P_{MS}(m) dm$ , we have for case A:

$$P(t) = \frac{m^3}{2C} P_{MS}(m) , \quad (11)$$

and for case B:

$$P(t) = \frac{m^{4.6}}{|2 \log m - 3.6|} \frac{1}{10^{1+(\log m)^2}} P_{MS}(m) \quad (12)$$

where we have dropped the subscript MS from the mass. The obtained age distributions are shown in Fig. 7 for Case A (solid curve) and B (dashed curve), respectively. Case A gives larger lifetimes for masses greater than one solar mass, which pushes the peak of the probability distribution to the right (2-3 Gyr), while for case B these lifetimes are shorter, and the peak moves to the left ( $\sim 1$  Gyr). Excluding the MS stars that do not lead to the formation of CSPN, the main effect on Fig. 7 is a sharp decrease in the probability for ages greater than about 12 Gyr, leaving the peak region essentially unaffected. The main conclusion that can be drawn is that a peaked distribution can be expected, but the precise location of the peak depends on the adopted initial mass-final mass relation and especially the calculation of the lifetimes.

For the sake of generality, we have also considered a quadratic relation as in Eq. (6) with  $c \neq 0$  instead of a linear equation. In this case, we have adopted the constants  $a$ ,  $b$ , and  $c$  from the recent work of Meng et al. (2008), taking the metal abundance  $Z = 0.02$ . The central star mass is given by the minimum of  $m_{CS}(a_1, b_1, c_1)$  and  $m_{CS}(a_2, b_2, c_2)$ , where  $a_1 = 0.5716$ ,  $b_1 = -0.04633$ ,  $c_1 = 0.02878$ ,  $a_2 = 1.1533$ ,  $b_2 = -0.2422$ , and  $c_2 = 0.04091$ . In this case, the probability  $P_{MS}(m)$  is given by  $P_{MS}(m) = (b+2cm_{MS}) P_{CS}(m)$ . As it turned out, the results of Fig. 7 are not particularly sensitive to this assumption.

### 3.2. The observed mass distribution of the central stars of planetary nebulae

The mass distributions of CSPN and white dwarfs have also been previously considered by Stasińska et al. (1997)

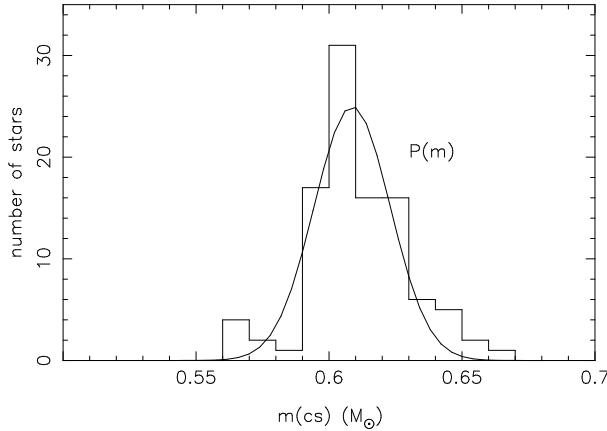
and Napiwotzki (2006). More recently, Gesicki & Zijlstra (2007) analyzed these distributions based on a dynamical method which allows mass determinations within  $0.02 M_\odot$  (cf. Gesicki et al. 2006). The CSPN masses were obtained for a sample of 101 objects from a relation between the temperatures of the central stars and the dynamical age of the surrounding nebulae. The ages were derived from a combination of recent spectra, line ratios and nebular sizes, using a photoionization model to obtain the central star temperature. Theoretical tracks by Blöcker (1995) were used to derive the stellar masses. It results that both the CSPN and white dwarf distributions peak around  $0.6 M_\odot$  as in Madej et al. (2004) and Stasińska et al. (1997), although the white dwarf distribution shows a broader mass range. The CSPN distribution shows essentially no objects with masses higher than  $0.7 M_\odot$ , while in the case of the DA white dwarfs, which are presumably the offspring of H-rich CSPN, a few objects are observed with masses larger than  $0.8 M_\odot$ . Although there may be some differences between the recently obtained white dwarf mass distributions, as discussed by Gesicki & Zijlstra (2007), they all agree in the sense that any sizable sample of CSPN is expected to have a larger number of objects with masses close to  $0.6 M_\odot$ . These results are in good agreement with our own N/O masses, as discussed by Maciel et al. (2008).

Instead of adopting the white dwarf mass distribution, we may then use directly the mass distribution of CSPN as recently derived by Gesicki and Zijlstra (2007). The mass distribution is shown in Fig. 8, and can also be approximated as a Gaussian probability density distribution similar to eq. (9), where we find  $A = 0.89627$ ,  $\sigma = 0.01431$ , and  $\mu = 0.6087$ . The corresponding probability distribution for CSPN is also shown in Fig. 8. Adopting again the same hypotheses as in Section 3.1, the CSPN age distributions are shown in Fig. 9 for Case A (solid curve) and B (dashed curve), respectively. In this case, the peaks are located at approximately 4-6 Gyr (Case A) and 2-4 Gyr (Case B).

## 4. Discussion

Some indication of the age distribution of CSPN may be obtained from the PN classification originally proposed by Peimbert (1976, 1990). According to this classification, the following approximate ages are attributed to the different PN types: Type I (1 Gyr), Type II (3 Gyr), Type III (6 Gyr), and Type IV (10 Gyr) (see for example Stasińska 2004, table 7). Type IV are halo objects, which are rarer and presumably much older than the remaining types, which are located in the disk and bulge of the Galaxy. Since nebulae of Types I-III constitute the vast majority of the known galactic PN, in this work we will not take into account the older, Type IV nebulae.

Fig. 7 shows the CSPN age distributions for Cases A and B using the mass distribution of white dwarfs (Madej et al. 2004), and Fig. 9 gives the corresponding distributions from the CSPN (Gesicki and Zijlstra 2007) mass distribution. The merged age distributions suggest a maximum around 2-6 Gyr for Case A and 1-4 Gyr for case B. Again, the main conclusion that can be drawn is that a peaked distribution can be expected, but the location of the peak depends on the adopted assumptions. In principle, we would expect Case B to be more realistic than Case A (see the discussion on stellar lifetimes by Romano et al. 2005), so that the results of Section 3 would suggest

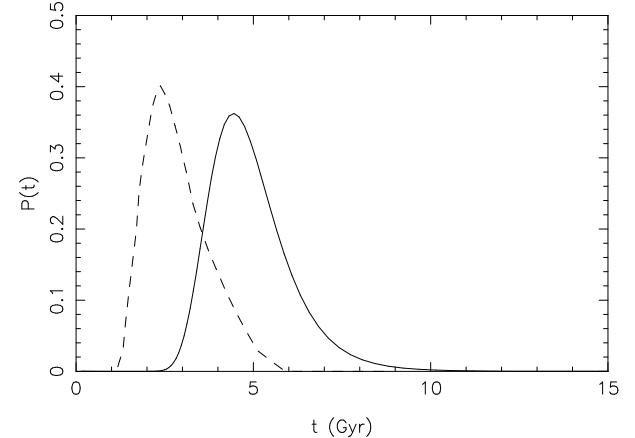


**Fig. 8.** Mass distribution of the central stars of planetary nebulae from Gesicki & Zijlstra (2007) and Gaussian fit.

a preferable range of 1-4 Gyr for the peak of the distribution. On the other hand, the results based on the empirical CSPN mass distribution are probably more accurate than those inferred from the white dwarf mass distribution, for the reasons mentioned in Section 3. Therefore, in view of these considerations, and taking into account the uncertainty analyses of Sect. 2.1c. and 2.2b., we suggest that the peak of the age distribution is probably located around 2-4 Gyr, as shown by the dashed curve of Fig. 9. We may then compare this distribution with the results of Sect. 2. Taking into account the uncertainties involved in the age determinations, which are estimated to be in the range 1.0-2.0 Gyr, approximately, as discussed in Sect. 2, it can be concluded that all methods considered produce results reasonably in agreement with the expected age distribution. According to the discussion in Sect. 2, Methods 1 and 2 have similar results, as indicated by Figs. 1 and 2, but the age distribution of Method 2 is less strongly peaked than either of the distributions obtained in Sect. 3 (cf. Figs. 7 and 9). Since the uncertainties are similar, Method 1 is probably more accurate than Method 2.

At face value, the age distributions of Method 3 shown in Figs. 3 and 4 are very similar to the results of Fig. 9, especially if Case B is considered, as seems more appropriate. In other words, the best results are probably those by Method 3, Case B (Fig. 4), which show a very good agreement with the results from the empirical mass distribution of CSPN, as shown by the dashed curve of Fig. 9. Although the estimated uncertainty of Method 3 is larger, it is reassuring that the average distribution shows such a remarkable agreement with the expected age distribution of CSPN. Therefore, our results obtained from completely independent methods and sources of data are reasonably in agreement with each other, so that we can have an estimate of the age distribution of CSPN. Naturally, the details of the individual age determinations still need to be worked out.

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**Fig. 9.** Age distribution of the CSPN progenitor stars from the observed mass distribution. Solid line: Case A, dashed line: Case B.

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